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The rate of convergence of positive linear operators in weighted spaces. (English summary)

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Given an unbounded, strictly increasing continuous function $\varphi: [0, +\infty) \rightarrow [0, +\infty)$ with $\varphi(0) = 0$ and φ^{-1} uniformly continuous, let $\rho = 1 + \varphi^2$ be a weight function and $B_\rho([0, +\infty))$ the space of all functions $f: [0, +\infty) \rightarrow [0, +\infty)$ for which there exists $M > 0$ such that $|f(x)| \leq M\rho(x)$ for every $x \geq 0$. This space will be endowed with the ρ -norm defined as $\|f\|_\rho := \sup_{x \geq 0} |f(x)|/\rho(x)$ ($f \in B_\rho([0, +\infty))$).

Moreover, consider the space $C_\rho([0, +\infty))$ of all continuous functions of $B_\rho([0, +\infty))$ and a sequence $(A_n)_{n \geq 1}$ of positive linear operators from $C_\rho([0, +\infty))$ into $B_\rho([0, +\infty))$.

The main result of this paper furnishes an estimate of the rate of the convergence

$$\lim_{n \rightarrow \infty} \|A_n f - f\|_\rho = 0 \quad \text{for every } f \in C_\rho^K([0, +\infty)),$$

where $C_\rho^K([0, +\infty)) = \{f \in C_\rho([0, +\infty)) : \lim_{x \rightarrow +\infty} f(x)/\rho(x) = K_f < +\infty\}$, by means of the modulus of continuity

$$\omega_\varphi(f, \delta) := \sup\{|f(x) - f(t)| : x, t \geq 0, |\varphi(x) - \varphi(t)| \leq \delta\}.$$

An application of such an estimate to Szasz-Mirakyan operators is also discussed.

Reviewed by *Vita Leonessa*